

tischen Zusammenstellung als wahrscheinlichsten Wert 3608,0 XE. an, während alle Bestimmungen aus den folgenden Jahren etwas niedrigere Werte, 3607,5 bis 3607,1 XE. liefern. Die Unterschiede sind grösser, als dass sie durch Verschiedenheiten des Brechungseinflusses erklärt werden könnten. Am sichersten dürfte der van Bergen'sche Wert sein, der aus Messungen an einem Einkristall erhalten wurde. Die eigenen Ergebnisse kommen diesem Wert sehr nahe.

Der Absolutwert jeder Gitterkonstantenmessung ist noch mit dem Fehler der Wellenlängenmessung behaftet. Die Angabe der Wellenlänge für Ni-K α_1 -Strahlung (Eriksson, 1928) mit 1654,50 XE. ist genau auf $\pm 0,012$ XE. Dies bedeutet für die Gitterkonstante von Kupfer ein $\Delta a = \pm 0,026$ XE. Dieser Umstand ist zu berücksichtigen, wenn Gitterkonstanten, die mit verschiedenen Strahlungen bestimmt wurden, miteinander verglichen werden sollen. Zusammenfassend ist zu sagen, dass bei Angabe der Gitterkonstanten von Kupfer in XE. schon die erste Stelle hinter dem Komma nicht mehr ganz sicher ist.

Zusammenfassung

1. Eine bei Chrom und Kupfer beobachtete Häufigkeitsverteilung der Gitterkonstante verschwindet, wenn die Metalle im Hochvakuum bei Temperaturen in der Nähe des Schmelzpunktes entgast werden.

2. Infolge der 'natürlichen Spektrallinienbreite' kann nur der Reflexionswinkelbereich bis etwa $88\frac{1}{2}^\circ$ zur Messung ausgenützt werden; experimentell wären Interferenzen bis $89\frac{1}{2}^\circ$ beobachtbar.

3. Der Einfluss der Brechkorrektur auf die Genauigkeit einer Gitterkonstantenbestimmung an Vielkristallen wird untersucht und festgestellt, dass die durch den Brechungseffekt bedingte Unsicherheit grösser sein kann als der eigentliche Versuchsfehler.

Der Deutschen Forschungsgemeinschaft sind wir für die Unterstützung der Arbeiten zu Dank verpflichtet. Herrn Prof. Dr P. P. Ewald danken wir für anregende Diskussionsbemerkungen.

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Acta Cryst. (1953). **6**, 24

The Crystal Structure of Datolite

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(Received 7 May 1952)

The structure of datolite has been analysed by means of the two-dimensional Fourier syntheses supplemented by a (linear) three-dimensional synthesis, using oscillation and Weissenberg photographs. The unit cell has the dimensions $a = 4.84$, $b = 7.60$, $c = 9.62$ Å, $\beta = 90^\circ 09'$, and contains 4 HCaBSiO₅. The space group is $P2_1/c$. The structure, obtained by deciphering a Patterson projection, includes separate SiO₄ groups but may be described as superimposed sheets of linked O and O-OH tetrahedra around Si and B atoms held together by Ca atoms. It is pointed out that the structure of gadolinite can be derived from that of datolite by simple replacement of atoms.

Introduction

Datolite, together with gadolinite and homilite, forms a well-defined group of minerals whose structural type is yet to be determined. This group was once regarded

as including also euclase (Bragg, 1937, p. 162). However, although their space groups are the same, the lattice dimensions and cleavage of euclase and datolite differ considerably and we cannot deduce between

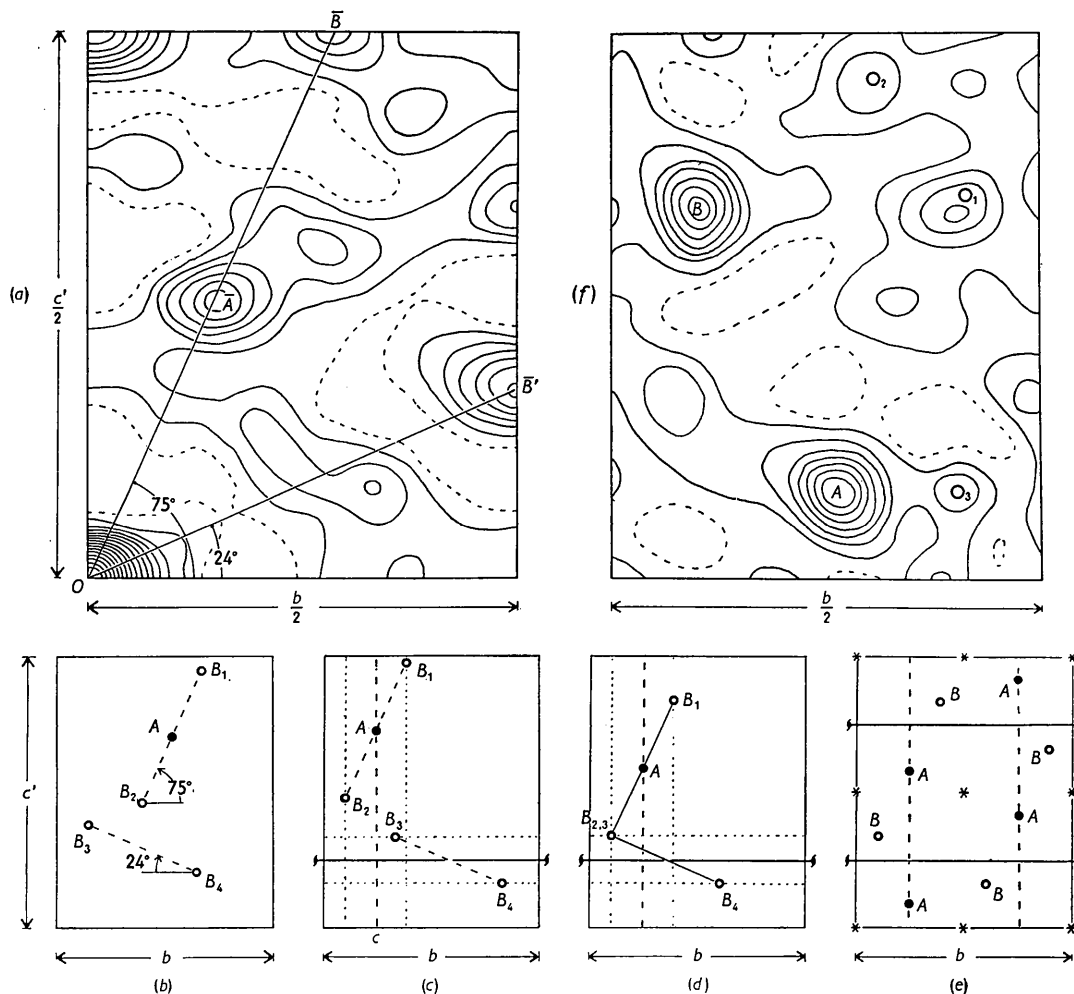


Fig. 1. Course of analysis illustrated. (a) Patterson projection on (100)'. (b)–(e) Steps to decipher (a) (see text, symmetry symbols as usual). (f) Fourier projection on (100)' (first synthesis).

them any reasonable relationship such as might be expected between kindred structures. The present study was undertaken to clarify the position of the datolite group in relation to euclase and other silicates.

Experimental

The specimens used in the study are short prismatic crystals from Bergen Hill, New Jersey, U.S.A. (Dana, 1900) having the typical composition of datolite, HCaBSiO_5 . They were kindly supplied by K. Sakurai.

Throughout the experiments, in which oscillation and Weissenberg photographs were taken, Mo or Cu $K\alpha$ radiations were employed. Intensities were estimated visually by means of the multiple-photographic technique, giving numerical values on an arbitrary scale. Only the Lorentz and polarization factors were taken into consideration.

The unit cell and space group

The unit cell has the dimensions

$a = 4.84 \pm 0.005$, $b = 7.60 \pm 0.01$, $c = 9.62 \pm 0.01$ Å (oscillation photographs, $\lambda = 0.710$ Å), $\beta = 90^\circ 09'$

(Dana, 1900, p. 504, morphological), and contains four molecules of HCaBSiO_5 . (We have also measured β on the Weissenberg photographs to be 90° within the experimental error.) The space group is $C_{2h}^5 - P2_1/c$. These observations are in agreement with the results obtained by Gossner & Mussgnug (1929) except that a and c are interchanged to conform to the axial ratio usually adopted.

Analysis

In the yz projection of the vector cell (Fig. 1(a)) we read at once that $O\bar{A} = \frac{1}{2}O\bar{B}$. This indicates that, in the corresponding projection of the atom cell (Fig. 1(b)), a heavy atom (say A) lies halfway between two other heavy atoms (say B_1, B_2). The length and orientation of B_1-B_2 are such that the two B 's are equivalent and subject to the glide plane c . The atom A must therefore lie on it (Fig. 1(c)).

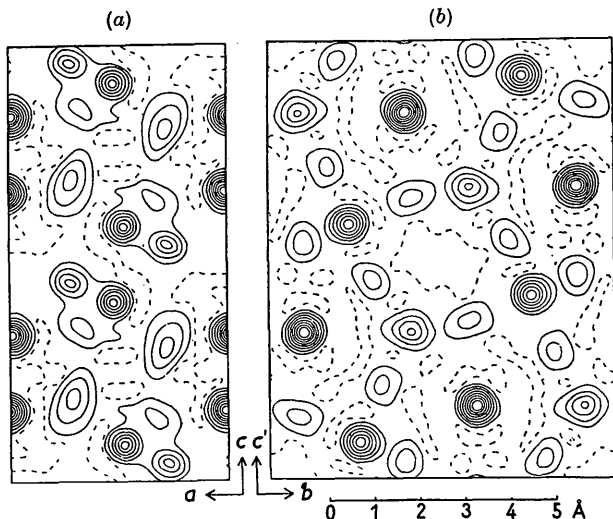


Fig. 2. Fourier projections of electron density on (a) (010) and (b) (100). Contours at intervals of $4 \text{ e.}\text{\AA}^{-2}$, the zero-electron lines being broken.

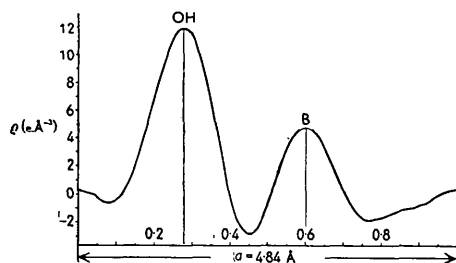


Fig. 3. Electron density along OH-B.

On the other hand, another pair of heavy atoms (say B_3, B_4 ; see Fig. 1(b)), corresponding to the vector OB' in the projected vector cell (see Fig. 1(a)), are again related to each other by a digonal screw axis (see Fig. 1(c)).

With these two restrictions simultaneously imposed, we may place B_2 and B_3 at the same point, as shown in Fig. 1(d). A complete set of four A 's and four B 's are then produced, as required by symmetry (Fig. 1(e)).

Since the major maxima of the vector map were satisfactorily accounted for by this distribution of heavy atoms we assumed that it represented a substantially correct picture of the structure. Silicon atoms were placed at A and calcium atoms at B , and F_{0kl} 's were calculated. The first Fourier summation was carried out using 30 experimental F_{0kl} 's* with the signs thus derived. (All these signs were subsequently proved to be correct.)

The result of the preliminary synthesis (Fig. 1(f)) indicated the positions of three oxygen atoms, in addition to those of calcium and silicon. The second summation was performed with 55 and the third with 95 terms. As refinement proceeded more peaks emerged in the electron-density map and we were able to read off from the fourth and final synthesis the y and z coordinates of all the atoms in the cell.

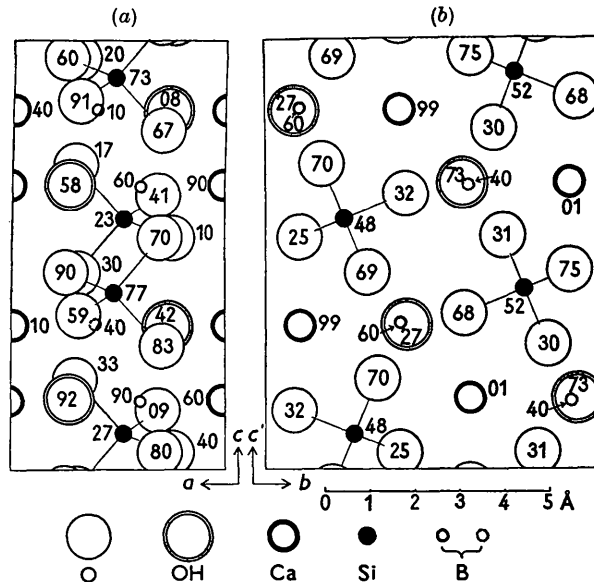


Fig. 4. The structure of datolite, projected on (a) (010) and (b) (100) (the figure corresponds to Fig. 2). Numbers give the height of each atom in the cell expressed as a percentage of the b and a translations.

In determining the remaining x coordinates the usual crystal-chemical concepts were utilized. The very short a length facilitated the location of atomic sites. The final decision, however, was reached after the completion of an xz Fourier synthesis, using experimental F_{h0l} 's*. Even this could not eliminate ambiguity as to the x coordinate of boron since it is overlapped by an oxygen atom in this projection. A three-dimensional summation along [100] passing the OH group and an boron atom was therefore resorted to:

$$\rho_{x,y,z} = \frac{1}{V} \sum^k \sum^h \sum^l F_{hkl} \cos 2\pi(hx/a + ky/b + lz/c),$$

where we put $y/b = 0.400$, $z/c = 0.340$.

The number of terms used was 668, F 's with $4 \sin^2 \theta/\lambda^2 > 1.50 \text{ \AA}^{-2}$ being cut off. The a length was subdivided into 60 parts, giving intervals of 0.08 \AA . For the summation F 's were multiplied by the tem-

Table 1. Coordinates of atoms

Atom	No. of equivalent atoms in the cell	x/a	y/b	z/c
Si	4	0.475	0.265	0.083
Ca	4	0.990	0.103	0.338
B	4	0.600*	0.400	0.340
O(1)	4	0.25	0.395	0.040
O(2)	4	0.69	0.300	0.460
O(3)	4	0.70	0.330	0.210
O(4)	4	0.32	0.085	0.140
OH	4	0.275*	0.415	0.335

* Results of the three-dimensional summation. The xz synthesis gave $x_B = 0.60$, $x_{OH} = 0.28$.

* Multiplied by the temperature factor, $\exp[-B(\sin \theta/\lambda)^2]$ with $B = 0.5 \text{ \AA}^2$.

Table 2. Observed and calculated F 's(a) Weissenberg photographs (Cu $K\alpha$)

hkl	F_o	F_c	hkl	F_o	F_c	hkl	F_o	F_c
002	10	-8	060	58	-64	20 $\bar{2}$	34	-36
004	58	-55	061	30	29	30 $\bar{2}$	10	-9
006	47	41	062	4	-4	40 $\bar{2}$	13	-6
008	33	-31	063	13	16	50 $\bar{2}$	9	-4
0,0,10	24	-26	064	31	41			
0,0,12	36	32	065	10	-12	10 $\bar{4}$	63	64
			066	15	-13	20 $\bar{4}$	78	-71
011	23	-15	067	12	12	30 $\bar{4}$	21	-36
012	3	-5	068	9	9	40 $\bar{4}$	38	-24
013	8	-2	069	10	-4	50 $\bar{4}$	—	2
014	52	-44						
015	18	-16	071	—	-2	10 $\bar{6}$	70	62
016	4	-6	072	12	-14	20 $\bar{6}$	4	8
017	9	6	073	10	6	30 $\bar{6}$	45	54
018	53	57	074	59	58	40 $\bar{6}$	13	12
019	7	12	075	14	-15	50 $\bar{6}$	48	38
0,1,10	5	-4	076	6	6			
0,1,11	9	-6	077	12	-12	10 $\bar{8}$	22	22
						20 $\bar{8}$	17	-17
020	25	-30	080	20	22	30 $\bar{8}$	10	-9
021	6	-7	081	19	12	40 $\bar{8}$	9	2
022	42	-38	082	2	5			
023	9	5	083	19	-18	1,0, $\bar{10}$	18	-20
024	13	-16	084	10	-16	2,0, $\bar{10}$	9	-1
025	70	65	085	19	-24	3,0, $\bar{10}$	42	-48
026	58	50	086	—	-1			
027	5	-6						
028	14	13	091	17	-24	110	2	-2
029	7	-11	092	14	-21	120	63	57
0,2,10	15	-22	093	10	16	130	66	-59
0,2,11	11	24				140	73	-60
						150	21	-20
031	12	17	100	20	-22	160	—	2
032	62	65	200	7	1	170	25	25
033	31	-34	300	71	60	180	9	3
034	40	-40	400	83	71			
035	12	12	500	4	-4	210	8	-4
036	16	-16	600	31	29	220	15	-19
037	8	-7				230	7	10
038	—	2	102	66	-72	240	12	13
039	—	-3	202	6	13	250	16	16
0,3,10	51	-47	302	72	-63	260	29	-32
0,3,11	11	6	402	10	3	270	17	-14
			502	41	-32	280	31	34
040	48	-54	104	66	-63	310	7	-2
041	34	-38	204	19	-26	320	24	30
042	38	38	304	13	11	330	49	50
043	11	-15	404	32	-21	340	53	-61
044	13	12	504	27	-26	350	—	-4
045	—	0				360	—	-6
046	59	-66	106	66	62	370	8	14
047	—	-7	206	10	-12	380	—	-5
048	—	2	306	78	74			
049	6	1	406	30	17	410	38	-27
0,4,10	40	34	506	36	31	420	9	-10
						430	35	-27
051	14	15	108	19	-23	440	35	-17
052	14	-22	208	—	-2	450	8	-1
053	10	8	308	—	7	460	38	-35
054	19	-22	408	47	-42			
055	19	20				510	34	-17
056	14	14	1,0,10	27	-35	520	31	26
057	12	17	2,0,10	—	5	530	26	14
058	9	10	3,0,10	16	-18	540	34	-30
059	27	-26	10 $\bar{2}$	12	-16	550	8	-10

THE CRYSTAL STRUCTURE OF DATOLITE

Table 2 (cont.)

(b) Oscillation photographs (Mo $K\alpha$)

hkl	F_o	F_c	hkl	F_o	F_c	hkl	F_o	F_c
111	46	-44	141	23	-27	17 $\bar{2}$	43	-45
112	52	56	142	—	3	17 $\bar{3}$	14	-14
113	63	64	143	22	19	17 $\bar{4}$	5	-1
114	14	24	144	35	34	17 $\bar{5}$	23	12
115	9	-10	145	40	35	17 $\bar{6}$	—	7
116	8	-7	146	10	-3	17 $\bar{7}$	19	14
117	15	-19	147	35	-30			
118	14	-12	148	33	30	181	19	24
119	30	28	149	—	0	182	16	-17
1,1,10	23	-24	1,4,10	—	11	183	9	6
1,1,11	—	-4				184	—	5
						185	24	-19
121	58	-56	151	23	24			
122	22	19	152	26	30	211	2	-3
123	56	57	153	58	-56	212	2	3
124	4	2	154	24	29	213	65	65
125	14	26	155	17	-14	214	70	-74
126	12	-16	156	11	-4	215	11	-16
127	40	-39	157	13	-2	216	—	-6
128	17	-13	158	16	-14	217	16	-23
129	—	-8	159	32	-30	218	30	33
1,2,10	—	0				219	29	34
1,2,11	26	26	161	14	13	2,1,10	11	11
			162	31	34	2,1,11	12	-10
131	26	27	163	14	-11			
132	—	2	164	8	-3	221	51	-44
133	20	-21	165	35	-33	222	22	-24
134	61	-51	166	25	-30	223	10	-12
135	28	17	167	23	18	224	—	1
136	30	-22	168	—	-6	225	29	21
137	37	22				226	20	22
138	47	47	171	4	-8	227	39	-46
139	19	-15	172	32	-35	228	—	7
1,3,10	18	14	173	4	-4	229	—	-2
			174	10	8	2,2,10	—	-5
11 $\bar{1}$	37	-32	175	17	15			
11 $\bar{2}$	61	66	176	9	4	18 $\bar{1}$	33	28
11 $\bar{3}$	52	48	177	—	14	18 $\bar{2}$	6	-8
11 $\bar{4}$	41	-27	14 $\bar{1}$	10	10	18 $\bar{3}$	33	21
11 $\bar{5}$	22	-22	14 $\bar{2}$	2	-7	18 $\bar{4}$	10	-4
11 $\bar{6}$	—	-5	14 $\bar{3}$	2	4	18 $\bar{5}$	15	-16
11 $\bar{7}$	36	-42	14 $\bar{4}$	24	22			
11 $\bar{8}$	9	-4	14 $\bar{5}$	27	20	21 $\bar{1}$	53	-49
11 $\bar{9}$	30	30	14 $\bar{6}$	—	-2	21 $\bar{2}$	—	2
1,1,10	28	-31	14 $\bar{7}$	—	-2	21 $\bar{3}$	57	56
1,1,11	—	2	14 $\bar{8}$	—	6	21 $\bar{4}$	23	-34
			14 $\bar{9}$	23	-19	21 $\bar{5}$	—	6
12 $\bar{1}$	62	-71	1,4,10	—	-2	21 $\bar{6}$	9	5
12 $\bar{2}$	14	14				21 $\bar{7}$	30	-35
12 $\bar{3}$	65	-72	15 $\bar{1}$	37	47	21 $\bar{8}$	30	29
12 $\bar{4}$	36	-32	15 $\bar{2}$	—	8	21 $\bar{9}$	20	19
12 $\bar{5}$	44	40	15 $\bar{3}$	48	-48	2,1,10	6	8
12 $\bar{6}$	27	-26	15 $\bar{4}$	29	19	2,1,11	—	-6
12 $\bar{7}$	29	-23	15 $\bar{5}$	27	22			
12 $\bar{8}$	24	-21	15 $\bar{6}$	5	0	22 $\bar{1}$	57	-56
12 $\bar{9}$	—	3	15 $\bar{7}$	39	36	22 $\bar{2}$	10	-13
1,2,10	19	11	15 $\bar{8}$	24	-18	22 $\bar{3}$	8	10
1,2,11	35	28	15 $\bar{9}$	30	-24	22 $\bar{4}$	38	39
						22 $\bar{5}$	20	20
13 $\bar{1}$	9	8	16 $\bar{1}$	10	11	22 $\bar{6}$	33	34
13 $\bar{2}$	28	26	16 $\bar{2}$	4	8	22 $\bar{7}$	42	-42
13 $\bar{3}$	2	-3	16 $\bar{3}$	14	-14	22 $\bar{8}$	—	3
13 $\bar{4}$	61	-53	16 $\bar{4}$	13	-4	22 $\bar{9}$	18	-21
13 $\bar{5}$	—	3	16 $\bar{5}$	35	-28	2,2,10	16	-16
13 $\bar{6}$	17	8	16 $\bar{6}$	37	-37			
13 $\bar{7}$	15	13	16 $\bar{7}$	27	20	231	—	-2
13 $\bar{8}$	49	46	16 $\bar{8}$	6	2	232	66	66
13 $\bar{9}$	18	-13				233	—	-3
1,3,10	15	-8	17 $\bar{1}$	—	-1	234	12	11

Table 2 (cont.)

<i>hkl</i>	F_o	F_c	<i>hkl</i>	F_o	F_c	<i>hkl</i>	F_o	F_c
235	11	-11	265	—	-10	331	10	-14
236	18	15	266	9	1	332	—	6
237	—	0	267	—	2	333	20	-23
238	21	22	268	—	8	334	63	-62
239	20	-17				335	14	11
2,3,10	31	-30	271	18	21	336	8	-9
			272	15	-15	337	10	8
241	—	-5	273	14	-13	338	18	-16
242	37	33	274	24	26	339	—	1
243	7	-7	275	—	-1			
244	17	14	276	—	6	341	26	-24
245	—	9				342	—	11
246	36	-37	281	21	20	343	9	-7
247	—	-8	282	—	-1	344	—	6
248	—	-8	283	—	-7	345	13	16
249	—	2	284	—	-13	346	15	-11
						347	10	-8
251	—	-9	311	10	-6	348	21	25
252	31	-29	312	37	37			
253	60	-67	313	20	17	351	31	36
254	12	-14	314	17	12	352	—	3
255	40	38	315	16	-16	353	—	-4
256	10	-12	316	22	16	354	18	17
257	39	33	317	21	-31	355	—	12
258	—	10	318	18	16	356	15	12
259	24	-22	319	9	12	357	12	13
			3,1,10	39	-36			
261	14	18				361	26	21
262	8	-6	321	45	-34	362	31	28
263	—	5	322	12	8	363	—	-5
264	14	14	323	42	-38	364	19	16
265	—	-8	324	—	-16	365	17	-19
266	8	4	325	43	39	366	39	-43
267	15	14	326	—	-6			
268	19	18	327	11	-11	331	—	3
			328	18	-21	332	11	-3
231	32	33	329	—	-4	333	27	-24
232	74	72				334	35	-36
233	11	-9	271	13	14	335	18	16
234	14	14	272	15	-14	336	—	-11
235	—	-6	273	14	-10	337	—	5
236	9	-11	274	24	22	338	46	46
237	16	17	275	—	-8	339	—	-7
238	14	12	276	—	0			
239	15	-9				341	22	-22
2,3,10	19	-17	281	11	10	342	14	9
			282	—	-4	343	12	8
241	28	-28	283	—	-2	344	62	58
242	22	23	284	—	-7	345	—	13
243	21	-20				346	—	-6
244	—	0	311	2	2	347	29	-26
245	15	26	312	58	49	348	—	2
246	52	-51	313	30	28			
247	—	-14	314	21	22	351	11	13
248	—	2	315	18	-16	352	22	25
249	—	6	316	22	-22	353	24	-24
			317	—	2	354	—	10
251	13	10	318	—	6	355	—	-7
252	36	-38	319	21	19	356	—	-4
253	57	-56	3,1,10	10	-14	357	—	-1
254	—	-6						
255	—	5	321	28	-24	361	—	6
256	—	-2	322	7	-3	362	—	4
257	30	29	323	11	10	363	—	-6
258	15	15	324	46	-42	364	15	18
259	20	-17	325	41	36	365	21	-14
			326	13	-10	366	23	-31
261	32	29	327	19	-12			
262	23	18	328	—	8	371	15	-14
263	18	24	329	12	-10	372	31	-30
264	—	13				373	9	-8
						374	13	14

Table 2 (cont.)

<i>hkl</i>	F_o	F_c	<i>hkl</i>	F_o	F_c	<i>hkl</i>	F_o	F_c
411	26	-23	421	8	-6	525	16	18
412	16	8	422	8	2	531	—	-2
413	13	18	423	35	-24	532	20	18
414	43	-30	424	8	6	533	—	-9
415	20	-16	425	41	36	534	39	-41
416	29	-22	426	18	21	535	—	1
417	10	-5	427	16	-18	451	34	28
418	15	15	431	—	7	452	23	-20
421	33	-29	432	52	51	453	22	-16
422	27	-26	433	21	-14	454	—	-8
423	33	33	434	33	-24	455	18	16
424	—	2	435	14	-9	461	26	16
425	19	27	436	19	-23	462	—	0
426	29	29	437	—	1	463	10	10
427	20	-20	441	—	-5	464	33	30
431	27	22	442	—	2	511	29	-29
432	37	32	443	11	-8	512	52	44
433	—	-9	444	—	-5	513	18	14
434	—	-8	445	12	12	514	17	-11
435	14	13	446	31	-29	515	7	-1
436	—	-1	447	17	9	516	19	-20
437	—	2	451	—	0	521	29	-28
441	26	-24	452	—	0	522	5	-6
442	37	29	453	32	-28	523	12	-14
443	—	0	454	17	-16	524	—	-13
444	13	9	455	16	12	525	21	18
445	—	7	461	26	23	531	20	9
446	39	-41	462	—	-2	532	16	16
447	17	-18	463	—	4	533	—	5
371	20	-16	464	—	2	534	—	-15
372	38	-40	511	—	1	535	—	4
373	11	7	512	19	17	541	—	-4
374	13	15	513	33	27	542	—	-5
411	22	-22	514	19	-9	543	—	13
412	14	-10	515	16	-13	541	—	2
413	21	22	516	13	12	542	—	6
414	51	-38	521	27	-25	543	—	-2
415	—	0	522	18	18			
416	11	4	523	—	12			
417	18	-18	524	—	4			
418	43	38						

perature factor $\exp[-B(\sin \theta/\lambda)^2]$ with $B = 0.5 \text{ \AA}^2$.

The two-dimensional Fourier maps of electron density are given in Fig. 2. Fig. 3 shows the result of the linear three-dimensional synthesis. The coordinates of atoms finally determined are given in Table 1. We give in Table 2 the F 's calculated on the basis of these parameters, compared with those experimentally determined. (The relative intensities were made comparable with those calculated by multiplying by a proportionality factor that minimized the sum of a certain number of the differences, $F_o - F_c$). The reliability number, $R = \sum ||F_o| - |F_c|| \div \sum |F_o|$, is 0.22 for all the reflexions observed.

The coordinates of calcium, silicon and boron atoms are considered accurate to within the experimental error of 0.01 Å and those oxygen atoms and OH groups to within 0.03 Å. The x coordinates of boron atoms and OH groups may probably be accurate to within 0.005 Å.

Description of the structure

The structure of datolite is illustrated in Fig. 4 (cf. Fig. 2).

Datolite is an orthosilicate containing separate SiO_4 groups. However, the structure may be conveniently described as superimposed complex sheets of linked oxygen and O-OH tetrahedra around silicon and boron atoms respectively.* In building up the sheet an Si-O and a B-O-OH tetrahedron alternate and form a ring of four tetrahedra on the one hand and one of eight tetrahedra on the other (Fig. 5). This mode of tetrahedral linkage is broadly the same with those found in apophyllite and other silicate minerals. The sheets are extended indefinitely parallel to (100) and

* The x coordinate of boron atom (0.600) reveals that it is almost at the centre of the O-OH tetrahedron ($x = 0.58$). It would have $x = 0.69$ if it were instead at the centre of the oxygen triangle.

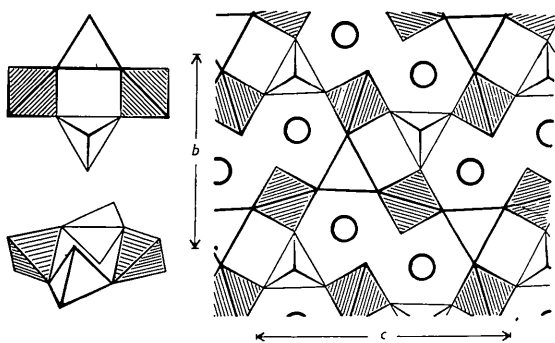


Fig. 5. The structure of datolite as linked tetrahedra of O and O-OH that make up a sheet (seen from the direction of the a axis). Ca atoms are shown by circles. SiO_4 tetrahedra are shaded and BO_3OH tetrahedra not shaded. Rings of four tetrahedra are singled out and drawn in projection and in perspective so as to make the reading of the figure easier.

held solidly together by calcium atoms which are in the middle of six oxygen atoms and two OH groups.

The balance of valency in the structure is illustrated in Fig. 6(a). The interatomic distances are given in Table 3.

Table 3. Interatomic distances

Atom	Neighbour	Distance (Å)	Atom	Neighbour	Distance (Å)
Si	O(1)	1.52	Ca	O(1)'	2.31
	O(2)*	1.66		O(1)*	2.30
	O(3)	1.69		O(2)	2.39
	O(4)	1.64		O(3)	2.55
B	O(2)	1.45	O(3)*	2.59	
	O(3)	1.44	O(4)	2.49	
	O(4)'	1.47	OH	2.71	
	OH	1.56	OH*	2.59	

O-O-OH distances in Å: O(1)-O(2)* 2.71, O(1)-O(3) 2.77, O(1)-O(4) 2.55, O(2)-O(3) 2.60, O(2)-O(4)'' 2.62, O(3)-O(4) 2.70, O(2)-O(3) 2.41, O(2)-O(4)' 2.37, O(2)-OH 2.49, O(3)-O(4)' 2.43, O(3)-OH 2.52, O(4)-OH 2.35.

* Atom of the neighbouring cell.

', '' Equivalent atoms.

The structure of datolite has apparently no relationship to that of euclase (Biscoe & Warren, 1933). It is to be noted that datolite has no conspicuous cleavage in spite of its sheet-like arrangement of atoms.

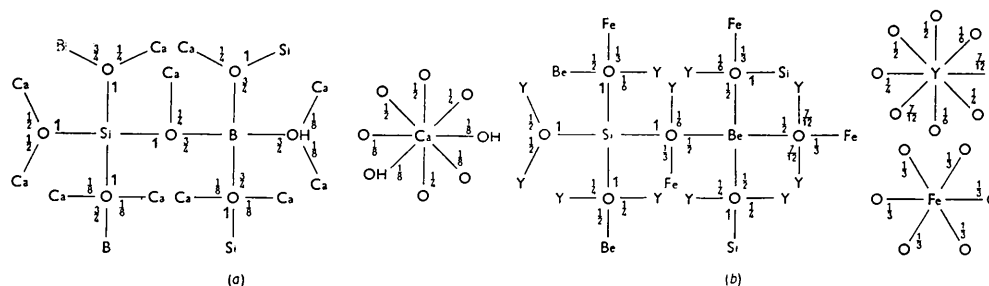


Fig. 6. Balance of bonds in (a) datolite and (b) gadolinite.

APPENDIX

On the structure of gadolinite

The structure of gadolinite may be derived from that of datolite simply by replacing calcium by yttrium, boron by beryllium and OH by oxygen and placing in addition iron at $0, 0, 0$; $0, \frac{1}{2}, \frac{1}{2}$. The balance of bonds will then be as perfectly maintained as in datolite (Fig. 6(b)). With these changes the co-

Table 4. Powder photograph of gadolinite (from Otomé, Japan)

Cu $K\alpha$ ($\lambda = 1.54$ Å). Camera radius 28.63 mm. $Q_0 = 4 \sin^2 \theta / \lambda^2$. $Q_c = h^2 a^2 + k^2 b^2 + l^2 c^2 + 2lhca \cos \beta$. $a = 4.71 \pm 0.01$, $b = 7.52 \pm 0.01$, $c = 9.89 \pm 0.01$ Å ($\lambda = 1.54$ Å), $\beta = 90^\circ 33'$ (morphological, Dana (1900), p. 509). $C_{2h}^2 - P2_1/c$. $Z = 2$ ($\text{Fe}_2\text{Y}_2\text{Be}_2\text{Si}_2\text{O}_{10}$). Intensities estimated visually.

hkl	Q_0	Q_c	I_0	$\frac{1}{2}F_c$
011	—	0.028	—	— 0.6
002	—	0.041	—	0.2
100	0.045	0.045	w	11.0
012	—	0.059	—	7.7
110	—	0.063	—	1.1
020	—	0.071	—	3.0
11 $\bar{1}$	0.072	0.073	vw	— 6.0
111		0.073	—	— 8.5
021	0.083	0.081	w	— 14.9
10 $\bar{2}$	—	0.086	—	— 0.5
10 $\bar{2}$	—	0.086	—	— 8.1
11 $\bar{2}$	0.104	0.104	—	22.1
112		0.104	s	22.1
013	0.110	0.110	w	20.1
022	—	0.112	—	— 2.4
120	0.117	0.116	w	26.8
12 $\bar{1}$	0.128	0.126	—	— 29.4
121		0.126	s	— 26.4
11 $\bar{3}$	0.155	0.155	—	31.4
113		0.155	s	35.5
12 $\bar{2}$		0.157	—	10.5
122		0.157	—	11.4
023	—	0.163	—	0.1
004	—	0.163	—	— 6.7
031	0.170	0.169	vw	15.6
200	—	0.180	—	11.2
014	0.182	0.181	m	— 17.5

ordinates of atoms given in Table 1 for datolite are applicable to gadolinite to the first approximation. The general agreement between F_c 's and F_0 's (obtained from powder photographs, Table 4) supports this view.

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Acta Cryst. (1953). **6**, 32

The Structure of the Free Radical di-*p*-Anisyl Nitric Oxide

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(Received 18 July 1952)

The unit cell of di-*p*-anisyl nitric oxide is orthorhombic, with $a = 7.33 \pm 0.04$, $b = 26.8 \pm 0.1$, $c = 6.25 \pm 0.03$ Å. The space group is *Aba2*, and in the unit cell there are four molecules, each lying on a twofold axis. The structure was solved by Fourier-transform methods, and the atomic positions, with bond lengths and angles, were found from the (100) and (001) Fourier projections.

Introduction

Di-*p*-anisyl nitric oxide is believed to be the first of the class of substances known as free radicals to be investigated by X-ray methods. This compound is quite stable, and the investigation, which depended largely on Fourier-transform methods, has presented no unusual difficulties.

Unit cell and space group

The sample supplied consisted of a mass of lath-like, red transparent crystals, from which it was not difficult to select single crystals suitable for X-ray examination. The unit cell was shown by oscillation photographs to be orthorhombic, and the unit-cell dimensions were found by considering the higher order $h00$, $0k0$ and $00l$ reflexions on *a*- and *c*-axis Weissenberg photographs. The results were:

$$a = 7.33 \pm 0.04, \quad b = 26.8 \pm 0.1, \quad c = 6.25 \pm 0.03 \text{ Å.}$$

A higher degree of accuracy is not claimed, since no allowance was made for film shrinkage.

The measured density of the sample was 1.33 ± 0.01 g.cm.⁻³, and the calculated density, corresponding to four molecules in the unit cell, was 1.32 ± 0.02 g.cm.⁻³.

The systematic absences were found to be: hkl for $k+l$ odd, $0kl$ for k odd or l odd, $h0l$ for h odd or l odd. These indicated the space group *Aba2* or *Abam*; packing considerations soon showed that the second of these was improbable, and the space group was assumed to be *Aba2*.

Determination of the structure

The X-ray intensities of the $hk0$ and $0kl$ zones were estimated by visual comparison of each Weissenberg

spot with a density wedge on similar film. The structure amplitudes were derived by using the usual trigonometrical factor; since the absorption coefficient of the substance was small, it was felt that further corrections were unnecessary.

The (100) projection, which showed the molecule roughly in plan, was solved by the Fourier-transform methods of Lipson & Taylor (1951). The problem was simplified by the fact that the space group *Aba2* has eight general positions, so that the four molecules were known to lie on twofold axes. In this projection, moreover, only one molecule had to be considered.

The projection was non-centrosymmetrical, and approximate phase angles were determined in a way which will be described in a subsequent paper on optical diffraction methods. The Fourier plot corresponding to these phase angles resolved every atom, and the projection was refined in the usual way by means of successive Fourier syntheses. This process was carried only as far as the fifth synthesis, as it then appeared that the suggested changes were becoming aimless. The (001) projection, which was centrosymmetrical, was then solved almost immediately by conventional methods.

Discussion of the structure

In Table 1 are given the atomic positions consistent with both projections, while in Tables 2 and 3 are compared the observed and calculated structure factors for the $0kl$ and $hk0$ zones. All the structure-factor calculations were carried out by the method of Beevers & Lipson (1952), using Fourier strips. The factor of agreement $R = \frac{\sum |F_o| - |F_c|}{\sum |F_o|}$ is 0.15 for the $0kl$ zone, and 0.19 for the $hk0$ zone, although, if accidental absences in the zone are not considered,